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Editor's Choice

AFLOW-ML: A RESTful API for machine-learning predictions of materials properties



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ABSTRACT

Machine learning approaches, enabled by the emergence of comprehensive databases of materials properties, are becoming a fruitful direction for materials analysis. As a result, a plethora of models have been constructed and trained on existing data to predict properties of new systems. These powerful methods allow researchers to target studies only at interesting materials – neglecting the non-synthesizable systems and those without the desired properties – thus reducing the amount of resources spent on expensive computations and/or time-consuming experimental synthesis. However, using these predictive models is not always straightforward. Often, they require a panoply of technical expertise, creating barriers for general users. AFLOW-ML (AFLOW Machine Learning) overcomes the problem by streamlining the use of the machine learning methods developed within the AFLOW consortium. The framework provides an open RESTful API to directly access the continuously updated algorithms, which can be transparently integrated into any workflow to retrieve predictions of electronic, thermal and mechanical properties. These types of interconnected cloud-based applications are envisioned to be capable of further accelerating the adoption of machine learning methods into materials development.

1. Introduction

Since their inception, high throughput materials science frameworks such as AFLOW [1–8] have been amassing large databases of materials properties. For instance, the AFLOW database [9–12] alone contains over 1.7 million material compounds with over 170 million calculated properties, generated from the <u>Inorganic Crystal Structure</u> <u>Database</u> (ICSD) [13–15], as well as by decorating crystal structure prototypes [16]. Combined with other online databases and highthroughput frameworks such as the Materials Project [17–20], NoMaD [21], OQMD [22,23], the Computational Materials Repository [24,25], and AiiDA [26,27], materials data is abundant and available. As a result, <u>m</u>achine <u>l</u>earning (ML) methods [28–30] have emerged as the ideal tool for data analysis [31–38], by identifying the key features in a data set [39] to construct a model for predicting the properties of a material. Recently, several models were developed to predict the properties of various material classes such as perovskites [40,41], oxides [42], elpasolites [43,44], thermoelectrics [45–47], and metallic glasses [48]. Additionally, generalized approaches have been devised for inorganic materials [49–60] and for systematically identifying efficient physical models of materials properties [61].

While predictions are powerful tools for rational materials design, the discipline is still reasonably new within the realm of materials science. As a result, a working understanding of machine learning principles, along with a high level of technical expertise, is required for using code bases effectively. This inhibits accessibility, where an average end user aims to utilize the codes to retrieve predictions with as little complication as possible. With the ever increasing number of predictive models, a unique challenge emerges: how does one create an accessible means to integrate machine learning frameworks into a materials discovery workflow?

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AFLOW-ML alleviates this issue by providing a simplified abstraction on top of sophisticated predictive models. Predictions are exposed through a web accessible <u>Application Programming Interface</u> (API) where functionality is distilled down to its essence: from the user input, return a prediction. AFLOW-ML can be added into any code base through use of an HTTP request library, native to most languages. Alternatively, AFLOW-ML can be utilized through use of the included Python client and command line interface. Through such abstractions, AFLOW-ML is accessible to a wide audience: it unburdens the user from having to understand the intricacies of machine learning and eliminates the technical expertise required to set up such codes.

2. REST API

The AFLOW-ML API is structured around a <u>REpresentational State</u> <u>Transfer (REST)</u> architecture, which allows resources to be accessed using HTTP request methods. Each resource is located at an endpoint, which is identified by a URL comprised of descriptive nouns.

A URL may also include special variables in the form of path parameters and a query string. A path parameter is a segment of the URL that specifies a particular resource and is denoted by a noun within braces ({...}) inside the endpoint. The query string is a list of key-value pairs placed at the end of a URL, which controls the representation (e.g. format) of the resource. Typically, it is used to apply filters or define the structure of the returned representation.

Resources within the API are represented in <u>JavaScript</u> <u>O</u>bject <u>N</u>otation (JSON), and are referred to as objects. Once at an endpoint, the user must specify how to interact with the object. This is referred to as an action, and is an HTTP request method. The API supports the two most common HTTP request methods, GET and POST, where GET fetches an object and POST sends user defined data to the server. Therefore, users interact with the API by performing actions (GET, POST) on endpoints (URLs) to retrieve objects (resources).

3. API structure

The overall structure of the API can be seen in Table 1. All endpoints are located at the base URL http://aflow.org/API/aflow-ml/v1.0/ and are organized by the model and the returned object.

AFLOW-ML currently supports two models: <u>m</u>olar fraction <u>d</u>escriptor (mfd) [50] and property-<u>l</u>abeled <u>m</u>aterials fragments (plmf) [49]. It is designed to be extensible, and additional models will be added in the future as they are developed.

The mfd model [50] predicts the material properties based on the chemical formula only: the vector of descriptors has 87 components, each component b_i being the mole fraction of element Z_i in the compound (Z_1 is H, Z_2 is He, etc.). The model is built with nonlinear support vector machines [29] and a radial basis function kernel. The model is trained using a data set of 292 randomly selected compounds of the ICSD for which the vibrational properties are computed with DFT calculations. Pearson and Spearman correlations for *k*-fold cross-validation ($k = 5 \rightarrow 14$) are in excess of 0.9 for all predicted properties, while the mean average errors are 13.2 meV/atom (vibrational free energy) and 0.037 meV/(atom K) (vibrational entropy) and the root mean square errors are 18.8 meV/atom (vibrational free energy) and 0.052 eV/

Table 1

A list of all endpoints in the API. Actions specify the supported HTTP request method, endpoints define the URL and objects are the returned resource. An endpoint with $\{...\}$ denotes a path parameter.

Action	Endpoint	Object
POST	/plmf/prediction	Task
POST	/mfd/prediction	Task
GET	/prediction/result/{id}	Status or prediction

(atom K) (vibrational entropy). Further details on the model training and validation can be found in Ref. [50].

The plmf model [49] represents each crystal structure as a colored graph, where the atomic vertices are decorated by the reference properties of the corresponding elemental species. Topological neighbors are determined using a Voronoi tessellation, and these nodes are connected to form the graph. The final feature vector for the ML model is obtained by partitioning the full graph into smaller subgraphs, termed fragments in analogy with the fragment-based descriptors used in cheminformatics [62]. All plmf models are built with the Gradient Boosting Decision Tree (GBDT) method [30]. Models for electronic and thermo-mechanical properties were trained on 26.674 and 2.829 materials entries from the AFLOW repository. respectively. All models are validated through Y-randomization (label scrambling) and fivefold cross validation, with coefficient of determination (r^2) values in excess of 0.9 for most quantities, while the mean average errors are 0.035 eV (electronic band gap), 8.68 GPa (bulk modulus), 10.6 GPa (shear modulus), 35.9 K (Debye temperature), 0.05 $k_{\rm B}$ /atom (heat capacity at constant pressure) and 0.04 $k_{\rm B}$ /atom (heat capacity at constant volume), and the root mean square errors are 0.51 eV (electronic band gap), 14.3 GPa (bulk modulus), 18.4 GPa (shear modulus), 57.0 K (Debye temperature), 0.09 $k_{\rm B}$ /atom (heat capacity at constant pressure) and 0.07 $k_{\rm B}$ /atom (heat capacity at constant volume). Further details on the model training and validation can be found in Ref. [49].

In general, API usage involves uploading a material structure to a POST endpoint, < model > /prediction, and retrieving a prediction object from a GET endpoint, /prediction/result/{id}, as shown in the flowchart in Fig. 1. POST endpoints are responsible for the submission of a material structure for a prediction. In their request body, the file keyword is required. It must contain a string representation of the material's crystal structure, in POSCAR 5 format (the lattice geometry and atomic position input file for version 5 of the VASP DFT package [63,64]). Upon receiving a request, the response body returns a task object containing information about the submitted structure, which has the following format:

```
{
  "id": String,
  "model": String,
  "results_endpoint": String
}
```

When a material is posted to the API, a prediction task is created and added to a queue. Each task is assigned an identifier, the id keyword, used to fetch the prediction object at the endpoint referenced in the results_endpoint keyword. This endpoint, /prediction/ result/{id}, supports the GET method and requires the id as a path parameter. Depending on the status of the prediction task, the response body returns a status object or prediction object. When the task is still in the queue, the status object is returned:

```
{
  "status": String,
  "description": String
}
```

The status object details the state of the prediction task. The state is identified by the keyword status which takes one of the following values: STARTED, PENDING, SUCCESS and FAILURE, while a description of each status type is given by the description keyword. When attempting to retrieve the prediction object, it is best to poll the endpoint periodically to check the status. Tasks that are still within the queue are given the STARTED or PENDING status, while a completed task status reads SUCCESS. In instances where the uploaded file is incorrectly formatted, a failed task occurs, status: FAILURE. When the task is completed, the response contains the prediction object. The prediction object is an extension of the status object and contains different keywords depending on the model used. For plmf, the prediction object, known as a plmf prediction, takes the following form:



Fig. 1. A flowchart illustrating the typical use-case of the API. First a POSCAR file is posted to the < model > /prediction endpoint to retrieve a task object. The id field of the task object is used to poll the < model > /prediction/{id} for the status of the prediction. If the status field of the response equals SUCCESS then the prediction object is returned.

{

```
"status": String,
"description": String,
"model": String,
"citation": String,
"ml_egap_type": String,
"ml_egap": Number,
"ml_energy_per_atom": Number,
"ml_ael_bulk_modulus_vrh": Number,
"ml_ael_shear_modulus_vrh": Number,
"ml_agl_debye": Number,
"ml_agl_heat_capacity_Cp_300K": Number,
"ml_agl_heat_capacity_Cv_300K": Number,
"ml_agl_heat_capacity_Cp_300K_per_atom": Number,
"ml_aql_heat_capacity_Cv_300K_per_atom": Number,
"ml_agl_thermal_conductivity_300K": Number,
"ml_agl_thermal_expansion_300K": Number
```

}

The mfd model returns an mfd prediction object:

{

}

```
"status": String,
"description": String,
"model": String,
"citation": String,
"ml_Cv": Number,
"ml_Fvib": Number,
"ml_Svib": Number
```

The details of each object and their keywords are found in the List of API Endpoints and Objects section.

4. Using the API

The process to retrieve a prediction is as follows: First, the contents of a POSCAR 5 file, titled test.poscar, are uploaded to the submission endpoint. This can be achieved by using an HTTP library such as Requests (Python) [65], URLSession (iOS SDK) [66], HttpURLConnection (Java) [67], Fetch (JavaScript) [68] or using a command line tool such as Wget or cURL. For this example, cURL is used. The contents of the POSCAR are posted to the submission endpoint as follows:

curl http://aflow.org/API/aflow-ml/v1.0/plmf/

prediction --data-urlencode file@test.poscar where the --data-urlencode flag handles encoding the contents of the POSCAR, located in the current directory, and associating it to the file keyword. Note that as mentioned previously, the POST returns a JSON response including the task id. The task id is then used to poll the results endpoint:

curl http://aflow.org/API/aflow-ml/v1.0/prediction/ result/{id}

The status keyword is used as an indicator to determine if any additional polling is required. Depending on the status of the job, the endpoint returns either a task status object or a prediction object. If the status keyword's value is SUCCESS then no additional polling is required, since the endpoint returns a prediction object, which is an extension of the task status object.

5. List of API endpoints and objects

This section includes the details of each endpoint and object accessible in the API. Endpoint information contains the associated HTTP method, request parameters, request body data and response object for each endpoint. Object properties are listed along with their type and description.

5.1. Endpoints

- POST plmf/prediction
 - Description. Uploads the contents of a POSCAR 5 to retrieve a prediction using the <code>plmf</code> model.
 - Query parameters.
 - * file (required) The contents of the POSCAR 5.
 - Response format. On success, the response header contains the

HTTP status code 200 OK and the response body contains a task object, in JSON format.

- Example. curl http://aflow.org/API/aflow-ml/v1.0/plmf/ prediction --data-urlencode file@test.poscar
- POST mfd/prediction
 - Description. Uploads the contents of a POSCAR 5 to retrieve a prediction using the mfd model.
 - Query parameters.
 - * file (required) The contents of the POSCAR 5.
 - Response format. On success, the response header contains the HTTP status code 200 OK and the response body contains a task object, in JSON format.
 - Example.
 - curl http://aflow.org/API/aflow-ml/v1.0/mfd/
 prediction --data-urlencode file@test.poscar
- GET/prediction/result/{id}
 - *Description*. Fetches the status object or returns the prediction object when the task is completed.
 - Path parameters.
 - * id (required) The unique identifier retrieved from the task object on submission.
 - Query string arguments.
 - * fields A comma separated list of the fields to include in the JSON response object. Note that specified fields only affects the prediction object.
 - *Response format.* On success, the response header contains the HTTP status code 200 OK. If the task is still pending, the response body contains a task status object in JSON format. Upon completion the response body contains a prediction object in JSON format.
- Example.

curl http://aflow.org/API/aflow-ml/v1.0/ prediction/result/59ea0f78-4868-4a1e-9a20e7343f00907d

5.2. Objects

- Task
 - *Description*. Describes the task for a submitted prediction. Includes the unique identifier for the prediction and results endpoint.
 - *Keys*. * id
 - *Description*. The unique identifier of the prediction task. Used at the fetch prediction endpoint to retrieve the status of a prediction and return the results on completion.
 - Type. String.
 - * results_endpoint
 - *Description.* The path of the endpoint where the prediction task status and results are retrieved.
 - · Type. String.
 - * model
 - \cdot *Description.* The name of the machine learning model used to generate the prediction.
 - · Type. String.
 - Example.

```
{
```

"id":	"d29af704-06bf
	-4dc8-8928
	-cd2c41aea454",
"model":	"plmf",
"results_endpoint":	"/prediction/result/

```
d29af704-06bf
-4dc8-8928-
cd2c41aea454"
```

```
• Status
```

}

- Description. Provides the status of a (prediction) task.

```
– Keys.
```

- * status
 - Description. The status of the task. Takes the following values: STARTED, PENDING, SUCCESS and FAILURE. When a task is added to the queue its status reads PENDING. Once it reaches the top of the queue the status reads STARTED and the prediction will run. If the prediction is successful the status reads SUCCESS.
 - · Type. String.
- * Description
 - · *Description*. Describes the status of the task.
- · Type. String.

- Example.

```
{
   "status": "PENDING",
   "description": "The calculation is running"
}
```

- plmf prediction
 - Description. The results of the prediction using the plmf model. This is an extension of the task status object.

```
– Keys.
```

- * status
 - Description. The status of the task. Takes the following values: STARTED, PENDING, SUCCESS and FAILURE. When a task is added to the queue its status reads PENDING. Once it reaches the top of the queue the status reads STARTED and the prediction will run. If the prediction is successful the status reads SUCCESS.
 - · Type. String.
- * description
- · Description. Describes the status of the task.
- · Type. String.
- * model
 - · Description. The model used in the prediction.
- · Type. String.
- * citation
 - · Description. The DOI for the model's publication.
- · Type. String.
- * ml_egap_type
- Description. Specifies if the material is a metal or an insulator. Takes the following values: Metal, Insulator.
- · Type. String.
- * ml_egap
 - \cdot Description. The electronic band gap.
 - \cdot Units. eV.
 - · Type. Number.
- * ml_energy_per_atom
 - · Description. The energy per atom.
- · Units. eV/atom.
- · Type. Number.
- * ml_ael_bulk_modulus_vrh
- *Description*. The bulk modulus, trained on data calculated with the Automatic Elasticity Library (AEL) [69].
- Units. GPa.

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- · Type. Number.
- * ml_ael_shear_modulus_vrh
- \cdot Description. The shear modulus, trained on data calculated with AEL.
- · Units. GPa.
- · Type. Number.
- * ml_aql_debye
 - *Description*. The Debye temperature, trained on data calculated with the Automatic GIBBS Library (AGL) [70].
 - · Units. K.
 - · Type. Number.
- * ml_agl_heat_capacity_Cp_300K
 - \cdot Description. The heat capacity at 300 K and constant pressure, trained on data calculated with AGL.
 - · Units. $k_{\rm B}$ /cell.
 - · Type. Number.
- pressure, trained on data calculated with AGL.
- · Units. $k_{\rm B}$ /atom.
- · Type. Number.
- * ml_agl_heat_capacity_Cv_300K
- \cdot Description. The heat capacity at 300 K and constant volume, trained on data calculated with AGL.
- · Units. $k_{\rm B}$ /cell.
- · Type. Number.

```
* ml_agl_heat_capacity_Cv_300K_per_atom
```

- \cdot Description. The heat capacity per atom at 300 K and constant volume, trained on data calculated with AGL.
- · Units. $k_{\rm B}$ /atom.
- · Type. Number.
- * ml_agl_thermal_conductivity_300K
 - \cdot Description. The lattice thermal conductivity at 300 K, trained on data calculated with AGL.
 - \cdot Units. W/(m K).
- · Type. Number.
- * ml_agl_thermal_expansion_300K
- *Description*. The thermal expansion coefficient at 300 K, trained on data calculated with AGL.
- · Units. K^{-1} .
- · Type. Number.

– Example.

{

"status":	"SUCCESS"
"description":	"The job has
	completed.",
"model":	"plmf",
"citation":	"10.1038/
	ncomms15679",
"ml_egap_type":	"Insulator",
"ml_egap":	0.923,
"ml_energy_per_atom":	-5.760,
"ml_ael_bulk_modulus_vrh":	178.538,
"ml_ael_shear_modulus_vrh":	140.121,
"ml_agl_debye":	713.892,
"ml_agl_heat_capacity_Cp_300K":	23.362,
"ml_agl_heat_capacity_Cp_300K	
_per_atom":	2.333,
"ml_agl_heat_capacity_Cv_300K":	22.625,
"ml_agl_heat_capacity_Cv_300K	

```
_per_atom": 2.311,

"ml_agl_thermal_conductivity

_300K": 2.792,

"ml_agl_thermal_expansion_300K": 6.093e-05
```

}

- mfd prediction
 Description. The results of a prediction using the mfd model. This is an extension of the task status object.
 - Keys.
 - * status
 - *Description.* The status of the task. Takes the following values: STARTED, PENDING, SUCCESS and FAILURE. When a task is added to the queue its status reads PENDING. Once it reaches the top of the queue the status reads STARTED and the prediction will run. If the prediction is successful the status reads SUCCESS.
 - \cdot Type. String.
 - * description
 - · Description. Describes the status of the task.
 - · Type. String.
 - * model
 - \cdot Description. The model used in the prediction.
 - Type. String.
 - * citation
 - \cdot Description. The DOI for the model's publication.
 - Type. String.
 - * ml_Cv
 - · Description. The heat capacity at constant volume.
 - · Units. meV/(atom K).
 - · Type. Number.
 - * ml_Fvib
 - · Description. The vibrational free energy per atom.
 - · Units. meV/atom.
 - · Type. Number.
 - * ml_Svib
 - · Description. The vibrational entropy per atom.
 - · Units. meV/(atom K).
 - · Type. Number.
 - Example.

{		
	"description":	"The job has completed.",
	"model":	"mfd",
	"citation":	"10.1021/acs.chemmater.
		7b00789",
	"status":	"SUCCESS",
	"ml_Cv":	0.221,
	"ml_Fvib":	21.188,
	"ml_Svib":	0.211
}		

6. Python client

A Python client is available for the AFLOW-ML REST API that provides researchers and developers a means to integrate AFLOW-ML into their applications or workflows, such as AFLOW π [8]. The client includes the AFLOWmlAPI class which provides all the functionality needed to interface with the AFLOW-ML API, and can be downloaded at http://aflow.org/src/aflow-ml. From the client, a prediction is

retrieved by passing the contents of a POSCAR to the get_prediction method. The AFLOWmlAPI class can be incorporated into a Python framework using code similar to the example illustrated below.

```
from aflowml.client import AFLOWmlAPI
with open('test.poscar', 'r') as input_file:
   aflowML = AFLOWmlAPI()
   data = aflowML.get_prediction(
        input_file.read(),
        'plmf'
)
```

This method takes two arguments: poscar and model, where poscar is the content from the file test.poscar and model is a string specifying the model to use (plmf or mfd). This method returns a Python dictionary, in which the keys and respective predicted values are model dependent. For a list of each prediction object's key and value pair, please refer to the previous section.

The client's AFLOWmlAPI class includes two additional methods, submit_job and poll_job, that provide more control when submitting a prediction, and which can be used in place of the get_prediction method in the previous example. The submit_job method targets the < model > /prediction endpoint and returns the jobs task id. From the id, the job can be polled using the poll_job method which returns a prediction object upon completion. These methods are ideal for cases where the user would prefer to postpone polling to a later time.

7. Command line interface

Upon installation, the Python AFLOW-ML client provides a <u>command line interface (CLI)</u> titled aflow-ml. The CLI exposes all the functionality of the Python client and is targeted at users who are not familiar with Python or using REST APIs. To receive a prediction the path of the POSCAR 5 file is passed to the CLI as a positional argument. Additionally, the model type is specified via the --model flag:

```
aflow-ml test.poscar --model=plmf
```

By default, the CLI outputs the results to the terminal. The default functionality is modified by the use of additional flags. For instance, results can be saved to an out file by use of the -s flag:

```
aflow-ml test.poscar --model=plmf -s
```

where the predicted results are saved to a file titled prediction.txt. Additional flags exist which provide various levels of customization such as specifying the predicted values to return or the format of the output. A list of each flag is found below. This list is also viewable from the CLI using the -h or --help flags.

7.1. CLI flags

Model

```
- Flag. -m or --model
```

- *Description.* (Required) Specifies the model to use in the prediction.
- Example.

```
aflow-ml test.poscar --model=plmf
• Save
```

```
- Flag. -s or --save
```

- Description. Saves the prediction to a file. If the out file is not specified contents are saved to a file named prediction.txt.
 Example.
 - aflow-ml test.poscar -m plmf -s

```
• Outfile
```

```
- Flag. -- outfile
```

- Description. Specifies the path and name of the out file.

```
- Example.
```

aflow-ml test.poscar -m plmf -s --outfile=prediction.txt

```
• Format
```

- Flag. --format
- *Description*. Specifies the format of the out file. Currently, text and JSON are supported.

```
– Example.
```

```
aflow-ml test.poscar -m plmf -s
--format=json
```

```
• Fields
```

```
- Flag. --fields
```

Description. State the predicted fields to show in the output.
 Expects fields as a comma separated list. If the flag is not present, all fields are shown.

– Example.

aflow-ml test.poscar -m plmf -s
 --fields=ml egap,ml egap_type

```
    Verbose
```

```
- Flag. -v or --verbose
```

- *Description*. Toggle verbose mode. When enabled the CLI logs the progress of the prediction.

```
– Example.
```

aflow-ml test.poscar -m plmf -v

8. Example applications

In order to demonstrate the utility of the AFLOW-ML API, two examples are provided, one each for the plmf and mfd models. These examples demonstrate how the API can be used to access machine-learning predictions, and to rapidly identify property trends for different classes of materials.

8.1. Predicting shear and bulk moduli for MoTi

For the first example, the AFLOW-ML API and the AFLOW data API are used to retrieve AFLOW-ML predictions for the shear and bulk moduli for the structures in the MoTi alloy system, which is one of the most populated binary alloy systems in the AFLOW database and is expected to form several ordered compounds [71]. Specifically, the shear and bulk moduli for the compositions that comprise the convex hull are investigated. First, the convex hull for MoTi is calculated using AFLOW via the following command:

```
aflow --chull --alloy=MoTi --output=json
```

The command outputs convex hull information in JSON format to the file aflow_MoTi_hull.json, containing an array of objects detailing information on each point in the convex hull as depicted in Fig. 2(a). Here, the points on the hull are extracted by filtering the array for entries in which the key ground_state is true.

Next, the AFLOW data API is used to fetch the <u>AFLOW Unique</u> <u>Identifier</u> (AUID) [11], species, stoichiometry and POSCAR for every MoTi entry in the AFLOW database.



Fig. 2. The predicted shear and bulk modulus for MoTi. (a) The convex hull for MoTi. (b and c) The predicted moduli vs. composition for all entries sharing a hull member composition, where the vertical bars indicate the range of values for all of the structures in AFLOW database for a given stoichiometry. (d and e) The distribution for equi-composition. (f) The predicted bulk modulus vs. the calculated formation enthalpy for each hull point composition.

```
import urllib2
import json
BASE_URL = 'http://aflowlib.duke.edu/AFLOWDATA
    # Fetch a list of all Mo Ti aflowlib entries
    \hookrightarrow by prototype
req = urllib2.Request(BASE_URL + '?
    \hookrightarrow aflowlib_entries')
res = urllib2.urlopen(req).read()
aflowlib_entries = res.replace('\n', '').split
    \hookrightarrow (', ')
print len(aflowlib_entries), " MoTi entries
    \hookrightarrow found"
print 'Fetching data:'
# For each entry get its json
entries_data = []
count = 1
for entry in aflowlib_entries:
    obj = \{\}
    obj['prototype'] = entry
    # auid
    reg = urllib2.Request(BASE_URL + '/' +
        \hookrightarrow entry + '?auid')
    res = urllib2.urlopen(req).read().replace(
        \leftrightarrow '\n', '')
    obj['auid'] = res
    # get species
    req = urllib2.Request(BASE_URL + '/' +
        \hookrightarrow entry + '?species')
    res = urllib2.urlopen(req).read().replace(
        \leftrightarrow '\n', '')
    obj['species'] = res.split(',')
    # get composition
    req = urllib2.Request(BASE_URL + '/' +
        \hookrightarrow entry + '?composition')
    res = urllib2.urlopen(req).read().replace(
        \hookrightarrow '\n', '')
    obj['composition'] = [int(d) for d in res.
        \hookrightarrow split(',')]
    # get stoichiometry
    req = urllib2.Request(BASE_URL + '/' +
        \hookrightarrow entry + '?stoichiometry')
    res = urllib2.urlopen(req).read().replace(
        \leftrightarrow '\n', '')
    obj['stoichiometry'] = [float(d) for d in
        \hookrightarrow res.split(',')]
```

```
# formation entropy per atom
    req = urllib2.Request(BASE_URL + '/' +
        ↔ entry + '?enthalpy_formation_atom')
    res = urllib2.urlopen(req).read().replace(
        \leftrightarrow '\n', '')
    obj['enthalpy_formation_atom'] = float(res
        \rightarrow)
    # sg relax
    reg = urllib2.Request(BASE_URL + '/' +
        \hookrightarrow entry + '?spacegroup_relax')
    res = urllib2.urlopen(req).read().replace(
        \hookrightarrow '\n', '')
    obj['spacegroup_relax'] = int(res)
    # POSCAR
    req = urllib2.Request(BASE_URL + '/' +
        \hookrightarrow entry + '/CONTCAR.relax')
    res = urllib2.urlopen(reg).read()
    poscar_lines = res.split(' n')
    poscar_lines.insert(5, ' '.join(obj['
        \hookrightarrow species']))
    poscar = ' \ n'.join(poscar_lines)
    obj['poscar'] = poscar
                                      %s'% (
    print '%s of %s
         count,
         len(aflowlib_entries),
         BASE_URL + '/' + entry
    )
    count += 1
    entries_data.append(obj)
print 'Writing to json'
with open('entries_data.json', 'w') as outfile
    \hookrightarrow :
    json.dump(
         entries_data,
         outfile,
         sort_keys=True,
         indent=2,
         ensure_ascii=False
    )
```

The resulting JSON file, <code>entries_data.json</code>, contains an array of objects holding the desir`ed set of information for each MoTi entry. Finally, each POSCAR is passed to the AFLOW-ML API client to retrieve the predictions.

```
from AFLOWml.client import AFLOWmlAPI
import json
with open('entries_data.json', 'r') as
   \rightarrow json_file:
    entries_data = json.load(json_file)
    predictions = []
    ml = AFLOWmlAPI()
    count = 1
    print "Fetching predictions:"
    for entry in entries_data:
        print '%s of %s
                                        %s'% (
            count,
             len(entries_data),
            entry['prototype']
        )
        count += 1
        prediction = ml.get_prediction(entry['
            \hookrightarrow poscar'], 'plmf')
        # merge entry and prediction dict
        merged = prediction.copy()
        merged.update(entry)
        predictions.append(merged)
print 'Writing predictions.json'
with open('predictions.json', 'w') as outfile:
    ison.dump(
        predictions.
        outfile,
```

```
)
```

Predictions are obtained from the plmf model and saved to the JSON file, predictions.json. This file also holds an array of objects, where each object contains the prediction results merged with the entry information found in entries_data.json. At this point, the AUIDs for each hull point, retrieved by filtering aflow_MoTi_hull.json, are used to identify their predictions found within predictions.json.

sort_keys=True,

ensure_ascii=False

indent=2,

The shear and bulk moduli vs. composition are plotted for each composition on the convex hull in Fig. 2. The top two panels (b and c) show the predicted moduli for each convex hull point (orange points) along with the range of predicted values for each entry that shares the same composition, while the bottom panels (d and e) display the distribution for equi-composition.

The plots in Fig. 2(b) and (c) indicate that the elastic moduli generally decrease with reducing Mo content. Furthermore, Fig. 2(d) and (e) demonstrate that while the range of predicted moduli for hull member compositions is large, the majority of predicted values cluster around the values for the entries on the hull. This suggests that the mechanical properties of the hull entries are generally representative of all entries sharing the same composition, and may also be partly due to the relaxation of many initial structures to the lowest energy one. Additionally, it is evident that the hull point bulk modulus values are always near the maximum predicted value, which is expected since it is known that this property correlates strongly with cohesive energy [53], of which the formation enthalpy is a component. This is supported by the strong dependence of the bulk modulus on the formation enthalpy for a given stoichiometry, as indicated by Fig. 2(f).

8.2. Vibrational free energy and entropy of perovskite oxides (ABO₃)

The second example leverages the mfd ML model to investigate the vibrational free energy and entropy for perovskite oxides (*ABO*₃). POSCAR files are generated using the aflow --proto command [16]:

aflow --proto=AB3C_cP5_221_a_c_b:A:0:B
--params=3.795 > AOB.poscar

where *A* and *B* are set for each combination of the following elements: Al, Si, S, P, Pd, Se, Ni, N, B, C, H, Ga, Pt, Sn, In, Ge, Er, Rh, Li, Zn, Te, K, Cu, Au, Ir, Ca, Ho, Br, Y, As, Pb, La, Ti, Sb, Bi, Cs, Ba, Tl, Cl, Co, Ce, Sr, Na, Rb, V, Cd, Ta and Sc. This results in 1126 POSCAR files, stored in a directory named POSCARS. Note that the generated POSCAR files are not in POSCAR 5 format and require conversion. Next, the AFLOW-ML API client is used to retrieve predictions for the vibrational free energy and entropy using the mfd model. As in the previous example, output is saved in JSON format to a file titled predictions.json.

import json import os from AFLOWml.client import AFLOWmlAPI predictions = [] ml = AFLOWmlAPI() for root, dirs, files in os.walk('POSCARS'): count = 1 for f in files: if f.endswith('.poscar'): print '%s of %s %s' % (

```
print 'Writing predictions.json'
with open('predictions.json', 'w') as outfile:
    json.dump(
        predictions,
        outfile,
        sort_keys=True,
        indent=2,
        ensure_ascii=False
)
```

Heat maps for each *AB* combination are plotted in Fig. 3 for the predicted vibrational free energy, F_{vib} , and entropy, S_{vib} . Two tendencies are visible: F_{vib} decreases and S_{vib} increases with atomic size; and local minima in F_{vib} and maxima in S_{vib} occur at compositions containing alkali metals. In general, heavy atoms with large radii result in lower vibrational frequencies, resulting in lower values of internal vibrational energy U_{vib} ($\sim \hbar \omega$), and higher values of S_{vib} . Since $F_{vib} = U_{vib} - TS_{vib}$, this results in F_{vib} having lower values for materials containing heavier atoms (towards the bottom right of the plot), as well as for compositions



H Li B C N Na Al Si P S CI K Ca Sc Ti V Co Ni Cu Zn Ga Ge As Se Br Rb Sr Y Rh Pd Cd In Sn Sb Te Cs Ba La Ce Ho Er Ta Ir Pt Au TI Pb Bi **Fig. 3.** The predicted vibrational free energy (a) and entropy (b) for perovskite oxides (*ABO*₃).

containing alkali metals that have large radii resulting in weak interatomic bonds and thus low vibrational frequencies. The inverse of this relationship is seen in panel (b), with maxima in $S_{\rm vib}$ occurring for

compositions containing alkali metals or very heavy elements such as Tl and Pb.

Rapidly generated plots such as these facilitate the discovery of

design rules, enabling the identification of suitable compositions for specific applications. It also provides insight into the criteria used by the machine-learning algorithms to predict materials properties.

9. Conclusion

AFLOW-ML enhances materials discovery by providing streamlined open access to predictive models. The REST API promotes resource sharing, where any application, workflow or website may leverage our models. Additionally, the Python client provides a closed solution, which requires little programming knowledge to get started. With this flexibility, AFLOW-ML presents the accessible option for machine learning in the materials design community.

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Appendix A. Data availability

The calculated data required to reproduce the convex hull in Fig. 2(a) and the structural input data for the AFLOW-ML API are available to download from http://www.aflow.org/ using the AFLOW data API [11], with detailed instructions provided in Section 8. The AFLOW-ML predicted data required to reproduce these findings can be generated and retrieved using the AFLOW-ML API from http://www.aflow.org/aflow-ml/, following the instructions provided in Section 8.

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